

CALCULATION OF DEVICES AND ELECTRONIC EQUIPMENT OWN NOISE (ACTIVE RC FILTER, RAUKH'S CIRCUITS)

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REZUMAT. Actuala lucrare este dedicată metodei de calcul a zgomotului propriu al dispozitivelor și echipamentelor electronice de selecție a semnalelor prin frecvență. Drept obiect ale acestor calcule sunt utilizate filtrele active RC, în varianta practică schemelor de realizare *Raukh*. Aceste scheme de realizare permit obținerea filtrelor active cu diferite funcții de transfer, ca trece-jos (FTJ), trece-sus (FTS) și trece-bandă (FTB). Metoda de calcul propusă în această lucrare este bazată pe un șir de elemente din teoria generală a cuadripolilor „zgomotoși”. Astfel, filtrul activ RC este prezentat ca o conexiune a doi cuadripoli, elementul activ (amplificatorul operațional) – sursă de tensiune comandată prin tensiune – STCT și circuitul pasiv RC, iar proprietățile lor de zgomot sunt prezentate ca un generator sumar I_{zz} (figure 5, a și b). Lucrarea conține rezultatele calculului teoretic conform metodei propuse și ale măsurărilor experimentale care confirmă posibilitatea utilizării acestei metode practice inginerescă (figure 8).

Cuvinte cheie: filtre active, funcție de transfer trece-jos, trece-sus, trece-bantă, amplificator operațional, cuadripol, zgomot propriu, zgomot termic, caracteristici de zgomot, densitatea spectrală, circuit echivalent, generator echivalent de zgomot.

ABSTRACT. This paper is dedicated to the method of calculation to its own noise of electronic devices and equipment for selection of signals by frequency. As the concrete object of the calculations presented in this paper are active RC filters in practice *Raukh* version. This scheme allows the realization of active filters to obtain the transfer function high-pass (HPF), low-pass (LPF) and pass-band (PBF). The calculation method proposed in this paper is based on elements of the general theory of quadripoles „noisy”. Thus, active RC filter is presented as a summary quadripole obtained from connecting the active element (operational amplifier) – voltage - controlled voltage source – VCVS and passive RC circuit, and a his noise properties – through a summary generator noise, I_{zz} (figure 5, a and b). The paper contains the results of theoretical calculations and experimental measurement, which confirm the possibility to utilize these methods of calculation in engineering practice (figure 8).

Keywords: active filter, pass-low, pass-high, pass-band transfer function, operational amplifier, quadripoles, own noise, thermal noise, noise characteristics, spectral density, equivalent circuit, noise equivalent generator

1. INTRODUCTION

Electronic noise can rightly be considered an obstacle to advanced technologies. From the category of „Advanced Technologies...” is part of Information Technology – perhaps even the most advanced technologies at the end of this century and the beginning of the millennium!

We can say with certainty that at present there is no other sphere of science and modern technology, which is experiencing a kind of rapid development. We are witness eyes of process that took place in the last decades of the twentieth century, a process that no one can be considered as an exaggeration....the computer

revolution, a process which reached its magic wing in absolute every human activity: economic and military, social and cultural, scientific and production activity.

This revolution is still ongoing and not long ago has entered a new phase, related to the WWW – *World Wi-de Web*, or already used – *Internet*, spider’s web.

Everything goes to the situation, it can in about 5 –7 years throughout the world there will be no people to whom fate and life would not be influenced by the pre-sence of this field world information or how far man should by computer and personal computers (PC).

The work began several generations of young professionals who were born, they mature and mental

enters formed in the century of personal computers. These generation can not imagine to life without a PC, as without a refrigerator, television or car. True is the fact that neither the car nor the TV do not occur as changes, modifications and even radical changes such compute: the operating methods or procedures of these devices or machines does not change significantly for decades.

Completely different things work for the computer: the computers entirely renewed about two years leads to a fundamental change in working methods and processes it. Who claims to meet the accelerated development of computer technology means constant selftraining needs and improve oneself. But for to use this technique to a genuine professional level it's required and more: a diligence work and constant effort, perseverance and unflinching desire to know what happens in the world of **information technology** [1].

The core of information technology is the working from electrical signals: a selection and reversion of these signals, processing and their transmission. Of particular importance in the information transmission and processing issues (which in turn is nothing more than data processing, id est of signal using appropriate mathematical instruments) the methods of calculation or mathematical modeling of both signal itself and the characteristics of items and devices, used in this purpose. Their-making process component characterizes the scientific and technical information of the technical means of calculation that is – without exaggeration – the foundation of progress worldwide.

Among the basic characteristics of computer components directly involved in signal processing it is considered the **sensitivity threshold** – at least that level of input signal, which can be plainly (and processed), the background **noise** – both foreign and **self**. This paper is dedicated to method of calculation to its own noise of the devices by selecting of signal for frequency, based on **active RC filters**.

These devices and electronic circuits are widely used in radio engineering, radio electronic and telecommunications, for the selection of signals by frequency, in equipments for multiplexing in plant liaison channels and in many other cases, when the frequency signal is in range of sound waves rather than of 1 MHz.

In this paper the author uses the notion of signal given in [2]: the signal is called a measurable physical quantity, carrier of information that can be remotely transmitted, received and/or processed.

2. CUADRIPOL „NOISY” ELEMENTS FROM THE GENERAL THEORY

In the paper is presents a method of noise analysis and calculation of its active *RC* filters (for *Raukh* realization circuit), in the construction version compatible with new technologies and requirements, using computer calculation methods.

The main idea of this method is that many of the elements, devices and even electronic assemblies – components of modern computing resources middle – may be regarded as dipoles, threepoles, quadri- and multipoles.

In the following are presented evidence of the general noise theory of linear quadripoles. On this basis are established the relations that allow determination of the summary noise property (the total effect of noise) as a summary and equivalent generator of current ($I_{Z\Sigma}$) or tension ($E_{Z\Sigma}$) of any quadripol, autonomous passive or non-autonomous activities, expressed by parameters Y or Z .

All linear amplification devices are part of non-autonomous active quadripols, that is why the analysis and calculations of these equivalent noise schemes quadripol's is of particular importance. The more so that in this class of quadripols are also and active *RC* filters.

The amplifiers and filters usually have a common input and output terminal, so that corresponding of general case of quadripol active, linear and non-autonomous.

For quadripols passive, as active and autonomous quadripols (Fig. 1) can write the following equality [3]:

$$Z_{12} = Z_{21}; Y_{12} = Y_{21}; H_{12} = -H_{21}, \quad (1)$$

characterizing symmetry (reversibility) them.

Therefore, to characterize such quadripol only three electrical parameters are enough. In the case of quadripols active but non-autonomous, because of inequalities

$$Z_{12} \neq Z_{21}; Y_{12} \neq Y_{21}; H_{12} \neq -H_{21}, \quad (2)$$

it's necessary (are required) four electrical parameters to describe their.

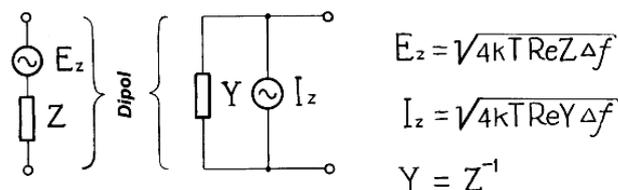


Fig. 1. Equivalent presentation noise properties of a dipol.

This condition is also valid for noise parameters: the minimum set of statistically independent noise parameters characterizing the time schedule, it is generally equal to the minimum set of independent electric parameters.

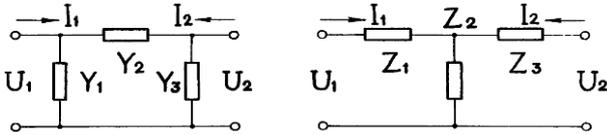


Fig. 2. II- and T-type schemes of the quadripols.

From the theory of circuits and systems is well known that any electrical circuit, how complicated it but that does not contain energy sources (ie passive) can be equivalently transformed into a scheme with a pair (di-pole, figure 1) or pairs (quadripole, figure 2) terminal.

If the circuit contains complex elements consisting of resistors, capacitors and in the general case - coils, then the properties of the noise can be described using the **thermal noise** equivalent generators.

So, for example the dipole can be presented as a generator equivalent of noise tension in series with the ideal (no noisy) resistance, or an equivalent current generator in parallel with the ideal conductance, as shown in figure 1.

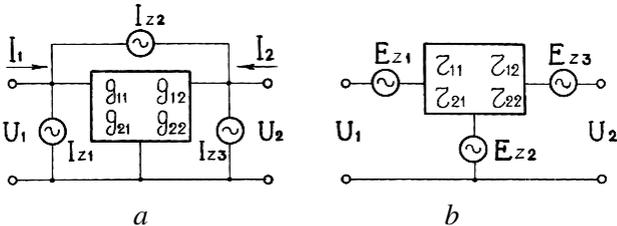


Fig. 3. Equivalent presentation noise properties of a quadripol.

The noise properties of autonomous quadripole with a common side (or terminal) can be externalized by three statistically independent noise parameters in the form of **generators noise voltages** or **noise currents**.

In accordance with those set out, in figure 3 shows the noise equivalent scheme of passive circuit. The electrical itself scheme in a form of quadripole with common terminal (and so...threepole) is given by parameters Y and Z . Given that in the „noisy” process real parties Y and Z are involved only, in figure 3 is presented the quadripole with her \mathcal{G} and r parameters.

The equations system, which connects the currents and voltages of input and output, if the scheme in figure 3 is:

$$I_1 = \mathcal{G}_{11}U_1 + \mathcal{G}_{12}U_2; I_2 = \mathcal{G}_{21}U_1 + \mathcal{G}_{22}U_2, \quad (3)$$

and for diagram of figure 3, b

$$U_1 = r_{11}I_1 + r_{12}I_2; U_2 = r_{21}I_1 + r_{22}I_2. \quad (4)$$

A particularly important concern in the calculation of noise have the equivalent transformation of the noise scheme, which ultimately simplifies the calculation and their analysis [4].

The equivalent noise generators in figure 3, a and b can be shown analytically (as thermal noise generator):

$$\overline{I_{Zi}^2} = 4kT \mathcal{G}_i \Delta f; \quad (5)$$

$$\overline{E_{Zi}^2} = 4kT r_i \Delta f, \quad (6)$$

where $i = 1 \div 3$,

$$\mathcal{G}_1 = \mathcal{G}_{11} + \mathcal{G}_{12}; \mathcal{G}_2 = -\mathcal{G}_{12}; \mathcal{G}_3 = \mathcal{G}_{22} + \mathcal{G}_{12}; \\ r_1 = r_{11} + r_{12}; r_2 = r_{12}; r_3 = r_{22} - r_{12}. \quad (7)$$

The ratio of noise parameters of the schemes in figure 3, a and figure 3, b is given by the relation [4]:

$$\overline{E_{Z1}^2} = \Delta r \cdot \overline{I_{Z3}^2}; \overline{E_{Z2}^2} = \Delta r \cdot \overline{I_{Z2}^2}; \overline{E_{Z3}^2} = \Delta r \cdot \overline{I_{Z1}^2}. \quad (8)$$

Voltage or current noise value from the corresponding equivalent generator can be calculated to using the equations (5) – (8). Practically, however, is more important to assess the effect of summary noise of any specific circuits. This summary noise effect in a form a brief summary current or a summary voltage can be determined to way consistent simplification of the schemes in figure 3, a and figure 3, b *id est* to moving from one equivalent scheme to another, more simpler.

An efficient method for simplifying analysis and calculations for the property noise of various schemes is the *method of transposition* of noise generators of voltage or current, from one sector of scheme to another, without changing the external noise effect of the scheme, in accordance with Thevenen well known theorem [4].

3. OWN NOISE CALCULATION OF RAUKH ACTIVE FILTERS RC

Any active filter RC (AF-RC) can be considered as a connection to *threepole*, passive and active. Where it follow the principles of the general theory of noise analysis and calculation of threepole considered above, are applicable in the case of own noise AF-RC.

For own noise analysis and calculation for AF-RC is required to achieve short-circuit condition or traveling in the van on the input terminals. Although these conditions carry a load abstract, they are still a convenient tool that simplifies the analysis and facilitate the noise calculation. The more so that all idealizations gravity that can be evaluated.

A dynamics (succession) of its noise calculation RC active filters will be presented on a particular case, the concrete acheme for practical realization, what is colled „scheme Raukh”, as the name of author *W. Raukh*. This scheme is frequently utilized in design and construction practice of active filter, with different functional characteristics [5]: HPF; LPF; PBF.

In figure 4 we can see the electrical scheme of active filter that carry low-pass function (LPF); HPF and PBF correspond to high-pass and band-pass function.

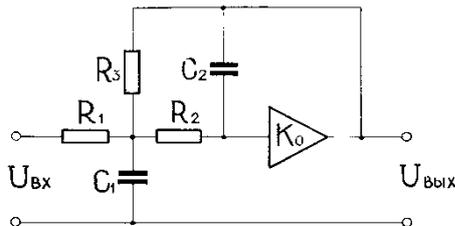


Fig. 4. Scheme of LPF Raukh.

From this scheme it is obvious that if the input terminals to provide a short-circuit regime, LPF can be considered as a parallel connection of two threepol, one of which is passive (RC circuit), the other – active (transistor, operational amplifier and for general – active element, figure 5, a).

Because each threepol may be presented by matrix of parameters $\|y\|$ and a properties of noise – with a summary equivalent noise generator I_{ZZ} , LPF filter may look to like as in figure 5, b.

The such presentation of LPF as a parallel connection of two threepol is convenient in the analysis phase of the circuits, but also indispensable for the calculation of noise takingm into account also the presence of feedback loop.

It is worth - while to note apart, even in not many works devoted for analysis and calculation of AF- RC noise, the presence of feedback loop or is not taken into account in general, or is specified in a form so relaxed, that it is equivalent with...ignored by her presence. Of course, it simplifies to a great extent the calculations, but not without injury to the degree of accuracy.

This presentation is more convenient from the point of view : allows the calculation of noise properties of active filters to employment of all possible means of matriciale algebra, which are widely used in various spheres of science and technology, allow computer resources tend implementation. Thia means (*software packages*) enjoys thesame succes, as for the case of synthesis of active RC filter as characteristics of amplitude-frequency and phase-frequency.

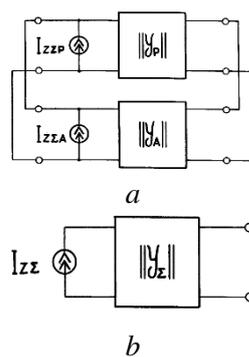
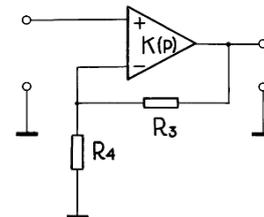


Fig. 5. Presentation of the LPF as connection of two threepols. Fig. 6. Operation amplifier as active element.



Thus, the active filter can be seen (and considered) as being one the active threepol generalised non-autonomous (figure 5, b), for which we can write:

$$\|y_{\Sigma}\| = \|y_A\| + \|y_P\|, \quad (9)$$

$$\overline{I_{ZZ}^2} = \overline{I_{ZZA}^2} + 2\xi \overline{I_{ZZA} I_{ZZP}} + \overline{I_{ZZP}^2}, \quad (10)$$

where ξ is the coefficient (or degree) of correlation between noise generators, I_{ZZA} and I_{ZZP} .

Mean square current $\overline{I_{ZZP}^2}$ – the summary effect of noise current of the passive threepol – depends entirely on the parameters $\|y\|$ of this threepol. The determination of these parameters does not present any difficulties in the terms of principle, although in some cases these expressions may be bulky and cumbersome. But...that's reality.

To calculation the current $\overline{I_{ZZA}^2}$ can be used the analytical relations obtained [4]. It should be mentioned that there is a serious difficulty: the calculation, and even the measuring of y parameters of the active threepol presents a uniquely process and in some cases it's simply impossible. Using an amplifier with two or three transistors as the active element its at actual cash is already an indication of bed taste, an aberration; is used as this the special integrated circuits – **operational amplifiers** (figure 6).

The basic advantages of an operational amplifiers (OA) is the high degree of stability and reproductive parameters and multiple functionality, a possibility to builde the active filter in a version of extreme micro-miniaturization, which is particularly important in the light of the problems they solve a modern microelectronic.

A two-transistor amplifier floor can be presented as an equivalent scheme which is described by squar matrix, of order 6, to operat such a matrix is quite difficult. This is great complexity in the presentation of

the operational amplifier through as one equivalent scheme and to execute equivalent transformation and calculation need later. On the other hand, the use of OA (worldwide occur in large series, for about...40 years) in the design and construction of active filter has become an imperative.

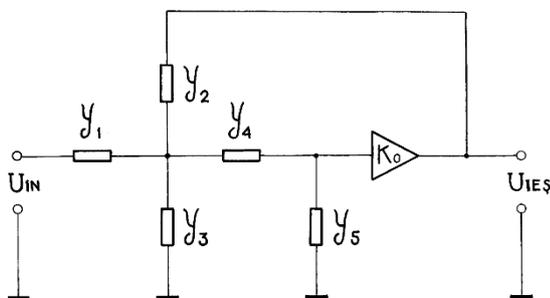


Fig. 7. General scheme to carry out the transfer function order 2, with VCVS.

Usually the technical sheet (or passport) accompanying the new OA not contain Y parameters, measuring of their encounters some experimental difficulties (a wide variety of these electronics devices and the absence instruments and universal method of measurement).

For the reasons stated above, the Y parameters are calculated in advance based on other technical data. For example, a typical data of every one OA (this store marking of similar devices in its original form, Russian and American – in brackets) mark KP544YД1 “Perara” (μ A741, company *Faichild Ins. Com.*):

- input resistance $Z_{IN} = 2 \cdot 10^5 \Omega$;
- the transfer tension coefficient (or amplifiere), with disconnected feedback $\sim 2 \cdot 10^4$;
- feedback coefficient equal to 0;
- output resistance $Z_{OUT} = 2 \cdot 10^2 \Omega$.

The physical meaning of these parameters are closer to the system \hat{h} parameters of quadripol. Therefore, we can write:

$$\begin{aligned} \hat{h}_{11A} &= Z_{INAO} = 2 \cdot 10^5 \Omega; \quad \hat{h}_{12A} = 0; \\ \hat{h}_{21A} &= 2 \cdot 10^4 \Omega; \quad \hat{h}_{22A} = 1/Z_{OUTAO} = 5 \cdot 10^{-3} \text{ S}. \end{aligned}$$

Using the matrices transformation, one can easily switch matrix Y , for which:

$$\begin{aligned} Y_{11A} &= 5 \cdot 10^{-6} \text{ S}; \quad Y_{12A} = 0; \\ Y_{21A} &= 2 \cdot 10^4 \Omega; \quad Y_{22A} = 5 \cdot 10^{-3} \text{ S}. \end{aligned} \quad (11)$$

Based on these data, using a method of calculation the own noise of active RC filters proposed in this paper and the experimental measurements were obtained satisfactory results in practical engineering design and

construction of devices for selection of signals by frequency. In figures above are the results of analytical calculations and experimental measurements [6] of its own noise spectral density $S_U = \varphi(f)$: LPF, scheme Raukh (figure 8).

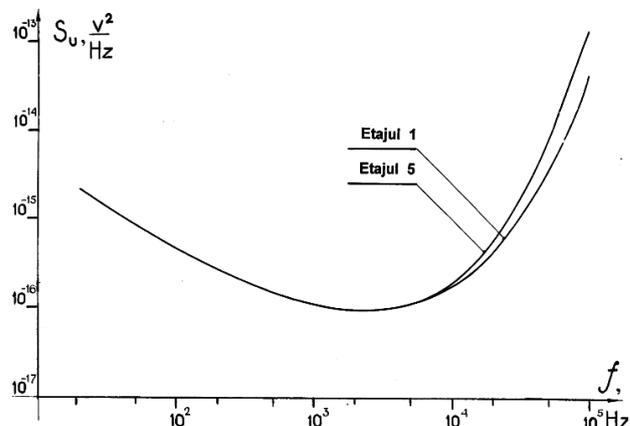


Fig. 8. Characteristics $S_U(f)$ of LPF Raukh.

The general scheme shown in figure 7, which carries transfer functions of order 2 is based on sources that when conductance VCVS $Y_3 = 0$ and Y_1, Y_2, Y_4, Y_5 are RC elements, such a scheme made LPF, HPF and PBF different versions, without signal inversion – *Sallen-Key* schemes [4], $K_0 > 0$; if $Y_3 \neq 0$ and $K_0 < 0$ we obtain the rings of order two, *Teyla* schemes. A special feature of these schemes is the fact that a single element made of the reaction loop and thus are schemes with a single feedback loop. But if the element Y_5 of passive RC circuit (figure 7) is not bonded but connected to the output of operational amplifier, thus obtained scheme already contains two elements of reaction Y_2, Y_5 and is called *multi-loop* reaction scheme.

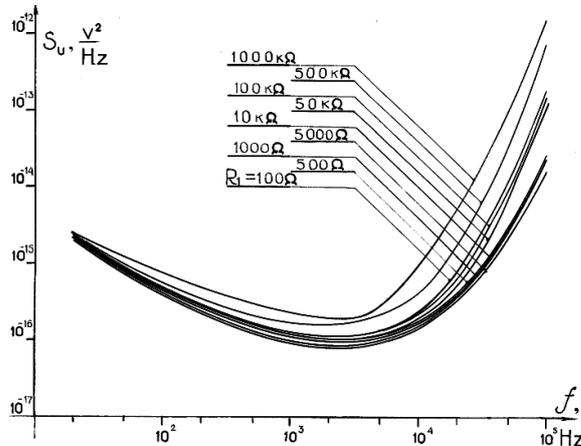


Fig. 9. Caracteristici $S_U(f)$ și $R_1 = \text{var.}$ (LPF Raukh, $K_0 < 0, f_i = 4,4 \text{ kHz}, U_{Z\text{șies}} = 15 \mu\text{V}$)

Active RC filter with multiple loop VCVS reaction that made LP, HP and BP transfer function with complex-conjugate pair of poles and zeros are in the complex plane axes origin or infinity, are known in engineering practice that the schemes *Raukh* (figure 4, 10 and 12). Operational amplifier in this case is reversed, noninverting input is connected to ground and $K_0 < 0$. Principal advantage of these schemes is very low output resistance, meaning that floors can be connected in cascade, without any mutual influence. But to obtain high values of quality factor Q is necessary a large scale sizes of scheme elements.

Of those exposed is obvious that in order to increase stability as well as to decrease sensitivity to changing circuit elements is reasonable that *Raukh* schemes to achieve limited amounts of quality factor ($Q \leq 5$, figure 14).

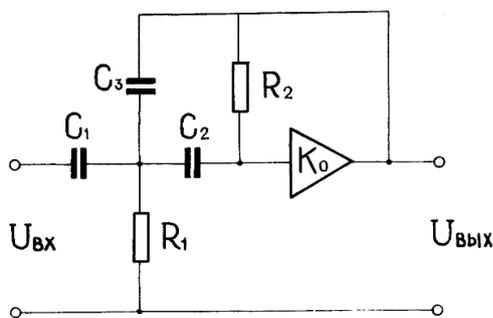


Fig.10. Scheme of HPF Raukh.

Computerized calculation method developed in this work and broadly described above allows to determine its dependence on the AF-RC own noise both the parameters and values of RC passive circuit elements ($y_1 \div y_5$), and the parameters of active elements (VCVS). In [4] is motivated choice of the noise spectral density $S(f)$ as an integral feature of the noise properties of active RC filters.

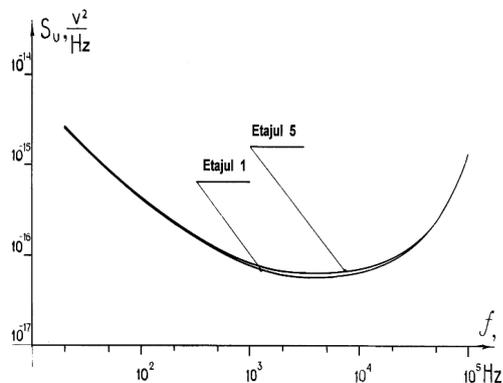


Fig. 11. Characteristics $S_U(f)$ of HPF Raukh.

Very important in the study of noise properties of active filters is to determine the dependence of these

properties of R and C values of passive circuits from figure 4. Voltage noise spectral density $S_U(f)$ depends, as is well shown in figures 9, 13 and 15, for concrete values of resistive element, this dependence is a quasi-parabolic with an extremum faintly.

On the other hand, a certain distribution and position of the set PZ (poles and zeros) of the transfer function can be achieved with different ratios of R and C passive elements, important as their product is constant: $R \cdot C = \text{const}$. Thus, there is a real opportunity to choose an optimal ratio of R and C in terms of noise properties, which allows less arbitrary and intuitive a choice the standardized resistance, \bar{R} [4].

For this is necessary to comply with certain requirements, according to [4] is reduced to the following conditions: any changes in RC parameters can take place only if

$$\left. \begin{aligned} \omega_0 &= \text{const} \\ 2\eta &= \text{const} \end{aligned} \right\}, \quad (12)$$

where

$$\omega_0 = \frac{1}{\sqrt{R_1 C_1 R_2 C_2}}$$

is the filter cutoff frequency;

R_1, C_1, R_2, C_2 – RC passive circuits elements (figure 4);

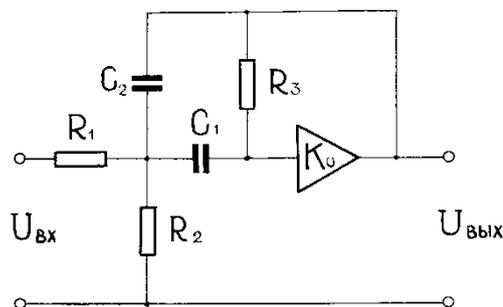


Fig. 12. Scheme of PBF Raukh.

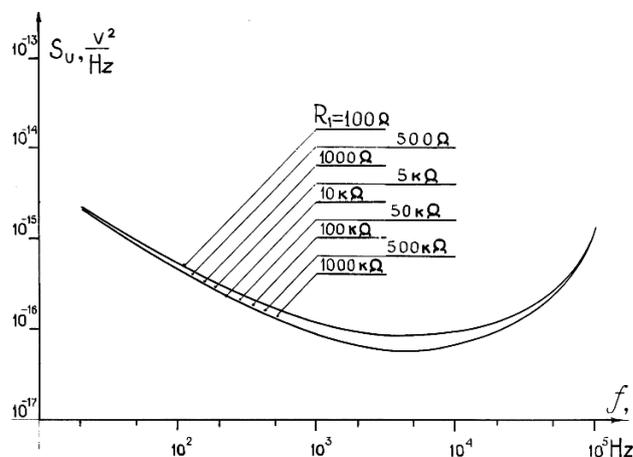


Fig.13. The characteristics $S_U(f)$ for $R_1 = \text{var}$. (HPF Raukh, $K_0 < 0$, $f_t = 4,4 \text{ kHz}$, $U_{Z\text{Zies}} = 10 \mu\text{V}$)

$$2\eta = \sqrt{\frac{R'}{C'}} + \frac{1}{\sqrt{R'C'}} + (1 - K_0)\sqrt{R'C'};$$

$$R' = \frac{R_1}{R_2}; C' = \frac{C_1}{C_2}.$$

Given these conditions, we performed theoretical calculations and computer analysis (Matlab function) of the FA's own noise-CR based schemes of achieving *Raukh*.

The results are presented in figures 8 and 9 (LPF), in figures 11 and 13 (HPF) and in figures 14 and 15 (PBF).

4. CONCLUSIONS

A study of the noise properties of Raukhala filters to revealed a some their peculiarities, namely:

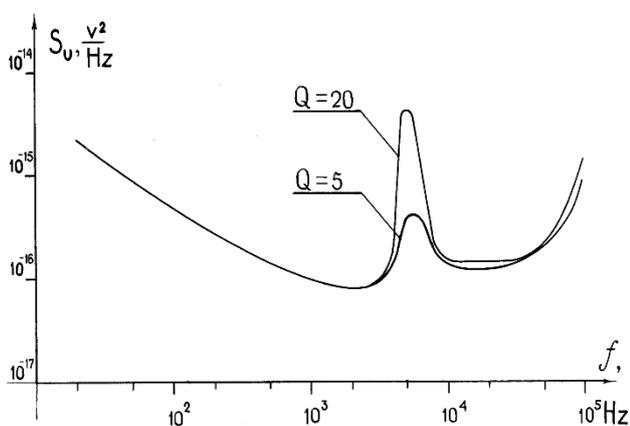


Figure 14. Characteristics $S_U(f)$ of PBF Raukh.

1. In the limited of band-pass, the output noise spectral density LPF (figure 8) and HPF (figure 11) does not depend on total from quality; the less noticeable dependence is observed for LPF on frequencies > 10 kHz, he can no only find the explanation in the Q factor of the stage, but in the frequency properties of the OA.

2. The most convenient in terms of noise values of R_1 , for Raukh LPF is $500 \Omega - 10 \text{ k}\Omega$. Values than this rise to a considerable increase in noise (figure 9).

3. The results obtained in the realization process of the PBF Raukh schemes, presents a contrast to those of *Sallen-Key* and *Teyla* schemes. Indeed, their LPF, HPF and PBF in the short circuit input terminals conditions, within the transition band did note (sharp) any increase of noise curves $S_U = \varphi(f)$ are smooth, without jumps. And these results are correct as long, as a quality of floor continuous low ($Q = 1,5 - 2$). Since only the quality of the floor begins to grow, takes place and growth (may be sudden) of noise, on cutoff frequency

f_t (for LPB or HPF), or control frequency (for PBF). This is for PBF Raukh to notes: it is enough quality value $Q = 5 - 6$, granting that the frequency ($f_0 = 4,4$ kHz) show a jump of $S_U = \varphi(f)$. If further Q increases, for example 4 times, this leads to increase in providing noise on control frequency by 10 times!

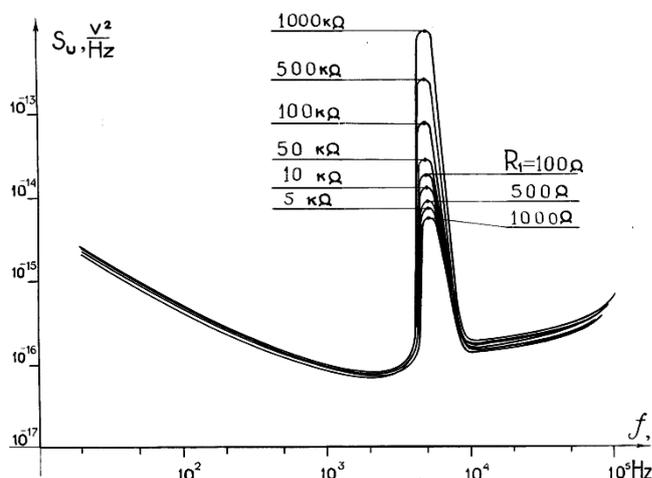


Fig. 15. The characteristics $S_U(f)$ for $R_1 = \text{var.}$ (PBF Raukh, $K_0 < 0$, $f_0 = 4,4 \text{ kHz}$, $U_{\Sigma \text{ies}} = 18 \mu\text{V}$)

4. From the characteristics $S_U = \varphi(f)$ depending on the values of passive circuit, that shows the output noise floor spectral density PBF does not depend basically of R_1 , only within the band crossing (figure 15). Within the band pass this dependence becomes significant and can reach 2 – 2,5 orders of magnitude (figure 15). The minimum amount of noise within the pass band, as well as the frequency range 20 Hz – 100 kHz corresponding to value $R = 1 \text{ k}\Omega$.

REFERENCES

- [1] V.Guțu, E.Guțu, Iu.Guțu, *Informatica. Partea I și Partea II*. Editura „TEHNICA INFO”, Chișinău 2008.
- [2] E.Ceangă and od., *Semnale, circuite și sisteme. Partea I*. Editura ACADEMICA, Galați 2001.
- [3] Е.П.Дементьев, *Элементы общей теории и расчёта шумящих линейных цепей*. Госэнерго - издат, Москва - Ленинград 1968 г.
- [4] V.Guțu, *Filtre active RC. Monografie*. Editura „TEHNICA INFO”, Chișinău 2009.
- [5] Л.Хьюлсман *Активные RC фильтры*. Издательство «Мир», Москва 1972 г.
- [6] <http://www.agir.ro/buletine/819.pdf>.

